

Method of consistent deformation of beams PDF

Method of consistent deformation of beams is a fundamental concept in structural engineering that plays a crucial role in analyzing and designing structural elements subjected to various loading conditions. This method allows engineers to determine the internal forces and moments within beams by considering their deformation compatibility, ensuring that the structure behaves as a cohesive unit. Unlike methods that focus solely on external loads and reactions, the method of consistent deformation emphasizes the relationship between the applied loads, the resulting displacements, and the internal forces, leading to more accurate and reliable analysis, especially in statically indeterminate structures.

Introduction to the Method of Consistent Deformation

The method of consistent deformation is based on the principle that, in a statically indeterminate structure, the deformations at certain points or sections must be compatible with the overall deformation pattern of the structure. This approach involves:

- Calculating the deformation of members under assumed internal forces.
- Ensuring compatibility conditions are satisfied.
- Solving for unknown forces or moments that maintain the structure's equilibrium and compatibility.

This technique is particularly useful when conventional methods like the force method (reciprocal deflection method) are cumbersome, especially in complex frameworks or continuous beams.

Fundamentals of the Method

Principles of Compatibility and Equilibrium

The core of the method of consistent deformation relies on two fundamental principles:

- **Equilibrium:** The internal forces and moments must balance the external loads.
- **Compatibility:** The deformations must be consistent and continuous across the structure, meaning that no overlaps or gaps occur between connected members.

By combining these principles, the method seeks to find a set of internal forces that produce deformations compatible with the boundary conditions and external loads.

Types of Deformations Considered

In the method, the primary deformations considered are:

- Bending deformations (deflections and rotations)
- Axial deformations (elongations and contractions)
- Shear deformations (less commonly considered in basic analyses)

Typically, for beams subjected primarily to bending, the focus is on deflections and rotations resulting from bending moments.

Step-by-Step Procedure for Applying the Method

Applying the method of consistent deformation involves several systematic steps:

1. Assume a Distribution of Internal Forces

Begin by assuming an initial distribution of internal forces or moments within the structure. These are often based on approximate methods or previous experience.

2. Calculate Deformations or Displacements

Using the assumed forces, compute the corresponding deflections and rotations at critical points. This is done through standard deformation formulas derived from material and geometric properties:

- For bending: $\delta = \frac{M \cdot l^2}{2EI}$ or more precise integration of the elastic curve.
- For axial deformation: $\delta = \frac{N \cdot l}{A \cdot E}$

where (M) is bending moment, (N) axial force, (E) Young's modulus, (I) moment of inertia, (A) cross-sectional area, and (l) length of the member.

3. Enforce Compatibility Conditions

Set up equations ensuring that the deformations are compatible with the boundary conditions and the overall deformation pattern of the structure. For example, in a continuous beam, deflections at supports must be compatible with zero or specified displacements.

4. Formulate and Solve Compatibility Equations

Express the compatibility conditions as a system of equations involving the unknown internal forces or moments. Solve these equations simultaneously to find the correct distribution of internal forces that satisfy both equilibrium and compatibility.

5. Verify and Refine

Check the calculated forces and deformations for consistency. If necessary, iterate the process with refined assumptions until the solution converges.

Application in Continuous Beams and Frames

The method of consistent deformation is especially powerful in analyzing continuous beams and frames where multiple supports and spans create complex internal force distributions.

Example: Continuous Beam Analysis

In a continuous beam with multiple spans subjected to uniform loads:

- Initial assumptions of moments at supports are made.
- Deflections at supports are calculated.
- Compatibility equations are established to relate these moments.
- Solving the system yields the actual moments and shear forces throughout the beam.

This approach ensures that the deformation compatibility conditions are satisfied, leading to more accurate internal force distributions.

Advantages of the Method of Consistent Deformation

The method offers several benefits for structural analysis:

- Provides an exact solution for statically indeterminate structures when combined with elasticity theory.
- Ensures deformation compatibility, leading to more realistic results.
- Effective in analyzing complex frameworks where other methods may be cumbersome.
- Facilitates the understanding of the relationship between loads, deformations, and internal forces.

Limitations and Considerations

Despite its strengths, the method also has certain limitations:

- It requires detailed calculations and iterative solutions, which can be time-consuming.
- Assumes elastic behavior; not suitable for plastic or non-linear analysis.
- Best suited for structures where deformation compatibility is critical.

Modern Computational Approaches

With advancements in computational tools, the method of consistent deformation is now often implemented through finite element analysis (FEA). Modern software can automatically perform deformation compatibility checks and solve large systems of equations, significantly reducing manual effort and increasing accuracy.

Summary

The method of consistent deformation of beams is a vital technique in structural engineering, emphasizing the importance of deformation compatibility in analyzing and designing indeterminate structures. By systematically assuming internal forces, calculating deformations, and enforcing compatibility conditions, engineers can accurately determine internal forces and moments, ensuring the safety and stability of structures. Whether applied manually for educational purposes or through sophisticated computational tools, the method remains a cornerstone in understanding complex structural behavior and achieving optimal design solutions.

Conclusion

Understanding and applying the method of consistent deformation is essential for structural engineers dealing with complex frameworks and continuous beams. Mastery of this technique enhances the capacity to analyze structures accurately, optimize material usage, and ensure safety standards are met. As structural systems become more sophisticated, integrating this method with modern computational methods will continue to be a vital aspect of structural analysis and design.

Method of Consistent Deformation of Beams: An In-Depth Analysis

The method of consistent deformation of beams stands as a cornerstone in structural analysis, providing engineers and researchers with a robust framework to understand and predict the behavior of beam structures under various loading conditions. Rooted in the principles of elasticity and compatibility, this method offers a systematic approach to solving complex problems involving bending, shear, and combined loading scenarios. This article delves into the theoretical foundations,

historical development, practical applications, and recent advancements related to the method of consistent deformation, offering a comprehensive review suitable for researchers, practicing engineers, and students alike.

Introduction and Historical Background

The study of beam deformation has evolved over centuries, from classical beam theories to sophisticated numerical methods. The method of consistent deformation emerged as a refinement of earlier techniques such as the elastic curve method and the moment distribution method. Its development was driven by the need for more accurate and reliable analysis of indeterminate structures, where traditional methods often fell short.

Historically, the early 20th century marked significant progress with the introduction of the flexibility method by Hardy Cross and later, the stiffness method. The method of consistent deformation was formalized as a way to satisfy compatibility conditions by iteratively adjusting assumed deformation parameters until equilibrium and compatibility were both satisfied—a process that aligns well with the modern finite element approach.

Theoretical Foundations

At its core, the method of consistent deformation is based on the principle of superposition and compatibility in elastic structures. It involves assuming a set of deformation parameters (such as deflections or rotations), calculating the resulting internal forces, and then adjusting these parameters iteratively until the deformations predicted by the assumed forces are consistent with the actual displacements.

The fundamental steps include:

- Assumption of deformation parameters: Usually, nodal displacements or rotations are initially guessed.
- Calculation of internal forces: Using the assumed deformations, the internal force distribution within the beam is computed via constitutive relations.
- Evaluation of equilibrium: The internal forces are checked against external loads to ensure equilibrium.
- Adjustment and iteration: Discrepancies between assumed and computed deformations prompt adjustments to the deformation parameters, repeating the process until convergence.

This iterative cycle ensures that the deformation state is compatible with the internal force distribution, satisfying the governing equations of elasticity.

Mathematical Formulation

Let us consider a beam subjected to a set of external loads $\{\mathbf{P}\}$. The method involves defining a vector of assumed deformation parameters $\{\boldsymbol{\delta}\}$, such as deflections and rotations at key points.

- The relationship between internal forces $\{\mathbf{F}\}$ and deformations is given by the flexibility matrix $\{\mathbf{f}\}$:

$$\{\boldsymbol{\delta}\} = \{\mathbf{f}\} \{\mathbf{F}\}$$

- Conversely, stiffness matrix $\{\mathbf{k}\}$ relates forces to displacements:

$$\{\mathbf{F}\} = \{\mathbf{k}\} \{\boldsymbol{\delta}\}$$

- Compatibility requires that the deformations computed from the internal forces match the assumed deformations:

$$\{\boldsymbol{\delta}\} = \{\mathbf{f}\} \{\mathbf{F}\}$$

- The iterative process adjusts $\{\boldsymbol{\delta}\}$ until the residuals are minimized, satisfying both equilibrium and compatibility.

Application to Beam Structures

The method is especially effective in analyzing indeterminate beams and frames, where multiple support reactions and internal forces exist. Its application involves:

- Identifying the redundant forces or deformation parameters.
- Computing the flexibility coefficients for the structure, often through influence functions or direct integration.
- Formulating equilibrium equations incorporating redundants.
- Iteratively refining the deformation assumptions until convergence.

This approach enables the resolution of complex statically indeterminate problems that are otherwise challenging with classical methods.

Example: Continuous Beam Analysis

Consider a continuous beam supported at multiple points under a uniform load. Traditional methods might involve complex calculations of moments and shear forces. Using the method of consistent deformation:

- Select redundant reactions or rotations at supports.
- Assume initial values for these redundants.
- Calculate deflections at key points based on the assumed redundants.
- Compute internal moments and shear forces.
- Check if the deflections satisfy boundary conditions.
- Adjust the redundants iteratively until deflections match boundary constraints.

This process results in an accurate distribution of internal forces and support reactions, ensuring the structure's compatibility.

Advantages and Limitations

Advantages:

- Applicability to indeterminate structures: Particularly suited for continuous beams, frames, and complex assemblies.
- Iterative refinement: Offers high accuracy through successive approximations.
- Compatibility with numerical methods: Forms a basis for finite element analysis and other computational techniques.
- Flexible in handling various loads and boundary conditions: Including point loads, distributed

loads, thermal effects, and more.

Limitations:

- Computational effort: Iterative procedures can be time-consuming, especially for large structures.
- Dependence on initial guesses: Convergence may be sensitive to initial assumptions.
- Complexity in multi-dimensional problems: Extending methods to 3D structures increases complexity.

Recent Developments and Modern Perspectives

The advent of computational tools has transformed the practical implementation of the method of consistent deformation. Modern finite element software incorporates these principles inherently, often automating the iterative process. Recent research has focused on:

- Enhancing convergence algorithms: Developing more robust iterative schemes to improve efficiency.
- Integration with nonlinear analysis: Extending the method to handle elastic-plastic behavior, large deformations, and time-dependent effects.
- Hybrid methods: Combining the consistent deformation method with other techniques such as the stiffness method or boundary element method for complex structures.

The method also finds applications in structural health monitoring, where deformation and force consistency are critical for assessing structural integrity.

Practical Considerations and Implementation

For engineers intending to apply the method of consistent deformation in practice, the following considerations are vital:

- Choice of redundant parameters: Selecting appropriate deformation parameters simplifies the analysis.
- Calculation of flexibility coefficients: Requires accurate influence functions or integration techniques.
- Convergence criteria: Defining acceptable thresholds for residuals ensures computational efficiency.
- Software tools: Modern structural analysis software (e.g., SAP2000, ANSYS, Abaqus)

incorporate these principles, but understanding the underlying method enhances interpretation and troubleshooting.

Conclusion

The method of consistent deformation of beams remains a fundamental approach in structural analysis, bridging classical methods and modern computational techniques. Its emphasis on compatibility and equilibrium offers precise insights into the behavior of indeterminate and complex beam structures. As structural systems grow more sophisticated, the method's adaptability and integration with numerical tools ensure its continued relevance. Future advancements will likely focus on improving computational efficiency, extending applicability to nonlinear regimes, and facilitating real-time structural health assessments.

By comprehensively understanding and applying the method of consistent deformation, engineers can design safer, more efficient, and more reliable structures capable of withstanding diverse loading scenarios and environmental conditions.

QuestionAnswer What is the method of consistent deformation in the analysis of beams? The method of consistent deformation is a structural analysis technique used to determine the internal forces and deflections in beams by ensuring that the deformation compatibility conditions are satisfied, often involving the use of flexibility matrices or stiffness methods. How does the method of consistent deformation differ from the direct stiffness method? While the direct stiffness method uses stiffness matrices to relate forces and displacements directly, the method of consistent deformation emphasizes ensuring that the calculated deformations are compatible with the applied loads and boundary conditions, often involving the use of flexibility matrices to achieve this consistency. What are the main steps involved in applying the method of consistent deformation to a beam problem? The main steps include: (1) calculating the flexibility coefficients for the beam, (2) applying loads to determine deformations, (3) setting up compatibility equations based on deformations, and (4) solving the resulting system to find internal forces and displacements. In what scenarios is the method of consistent deformation most effectively used? This method is most effective in statically indeterminate structures, such as continuous beams and frames, where compatibility conditions are essential to determine internal forces and deflections accurately. What are the advantages of using the method of consistent deformation for beam analysis? Advantages include its systematic approach to handling indeterminate structures, the ability to incorporate flexibility and deformation considerations directly, and providing accurate internal force and deflection predictions by ensuring compatibility conditions are met.

Related keywords: beam bending, deformation analysis, structural mechanics, elastic deformation, plastic deformation, finite element method, beam theory, deflection calculation, load distribution, mechanical engineering

REGULA FALSI METHOD ADVANTAGES AND DISADVANTAGES

Regula Falsi Method Advantages and Disadvantages

The regula falsi method, also known as the false position method, is a numerical technique used to find approximate solutions to equations where the root is unknown. It is a bracketing method that combines the features of the bisection method and the secant method, aiming to improve convergence speed while maintaining reliability. Like any numerical approach, it offers a set of advantages that make it appealing for certain applications, but it also exhibits notable disadvantages that can limit its effectiveness in specific scenarios. Understanding these benefits and drawbacks is crucial for practitioners to decide when and how to employ the regula falsi method effectively.

Advantages of the Regula Falsi Method

1. Guaranteed Convergence Under Certain Conditions

One of the primary advantages of the regula falsi method is its guaranteed convergence, provided that the initial interval brackets a root and the function is continuous. Since the method always maintains an interval where the function changes sign, it ensures that the root lies within the bounds during each iteration. This reliability makes it a safe choice compared to open methods like the secant method, which may not always converge.

2. Simplicity of Implementation

The regula falsi method is straightforward to implement computationally. Its core involves calculating a linear approximation between two points and updating the interval based on the sign of the function at the approximated root. The simplicity of the algorithm makes it accessible even for beginners and easy to incorporate into larger computational routines or software.

3. Faster Convergence Than the Bisection Method

Compared to the bisection method, which halves the interval in each iteration, regula falsi often converges more quickly because it uses a secant-like approach to estimate the root. By adjusting the interval based on a linear approximation, it tends to reduce the number of iterations needed, especially when the initial interval is well-chosen and the function behaves approximately linearly near the root.

4. Fewer Function Evaluations Than Bisection

While both methods require function evaluations at each step, regula falsi often achieves a desired

accuracy with fewer evaluations compared to bisection. This efficiency can be particularly valuable when function evaluations are computationally expensive or time-consuming.

5. Flexibility With Different Types of Functions

The method is applicable to a wide range of functions, including nonlinear and complex functions, as long as the initial interval brackets a root. Its reliance on linear approximation rather than derivatives makes it suitable even when derivative information is unavailable or difficult to compute.

Disadvantages of the Regula Falsi Method

1. Slow or Stagnant Convergence in Certain Cases

Despite its faster convergence relative to bisection, regula falsi can experience slow progress or stagnation, especially when the function exhibits certain behaviors. For example, if one endpoint of the interval is close to the root and the other is far, the method may repeatedly refine the approximation near one side without significantly improving the estimate overall. This phenomenon is known as "stagnation" and can lead to an impractical number of iterations.

2. Sensitivity to the Initial Interval

The effectiveness of the regula falsi method heavily depends on the choice of the initial bracketing interval. If the initial interval does not contain a root or is poorly chosen, the method may fail to converge or converge very slowly. The method requires a good initial approximation to be efficient and reliable.

3. Potential for Non-Progressive Iterations

In some cases, the method can get "stuck" or make negligible improvements over iterations. This occurs when the linear approximation becomes poor due to the nonlinear nature of the function, especially near inflection points or discontinuities. As a result, the method might oscillate or hover without substantial progress towards the root.

4. Not as Fast as Higher-Order Methods

Compared to methods like Newton-Raphson or secant methods, regula falsi generally converges more slowly because it is a bracketing method with linear convergence. For functions where derivative information is available and the function behaves well, higher-order methods can achieve quadratic or superlinear convergence, making regula falsi less efficient.

5. Computational Overhead in Some Variants

While the basic regula falsi method is simple, some advanced variants attempt to improve convergence by modifying how the new approximation is computed. These variants can introduce additional computational steps or complexity, which may negate some of the simplicity advantages of the original method.

Summary of Advantages and Disadvantages

Summary of Advantages

- Guaranteed convergence when the initial interval brackets a root
- Simple to implement and understand
- Generally faster than the bisection method
- Requires fewer function evaluations compared to bisection in many cases
- Applicable to a wide range of functions without needing derivatives

Summary of Disadvantages

- Can experience slow convergence or stagnation in certain functions
- Highly dependent on the choice of initial interval
- May get stuck or oscillate without significant progress
- Slower convergence compared to higher-order methods like Newton-Raphson
- Potential additional computational complexity in advanced variants

Conclusion

The regula falsi method remains a valuable tool in the numerical analyst's toolkit, especially when robustness and guaranteed convergence are prioritized over speed. Its advantages, such as simplicity, reliability, and efficiency, make it suitable for a variety of problems, particularly when derivative information is unavailable or the function is complex. However, its disadvantages, including potential stagnation and sensitivity to initial conditions, mean that practitioners should exercise caution and consider alternative methods if rapid convergence is necessary or if the function exhibits challenging behavior. Understanding the balance between these advantages and disadvantages allows for more informed method selection and more effective problem-solving in numerical root-finding tasks.

Regula Falsi Method Advantages and Disadvantages

The regula falsi method, also known as the false position method, is a popular numerical technique used for finding roots of continuous functions. This iterative method provides an efficient way to

approximate solutions to equations where analytical methods may be cumbersome or impossible. Its simplicity, combined with its ability to converge quickly under certain conditions, makes it a preferred choice among mathematicians, engineers, and scientists. However, like any numerical technique, the regula falsi method also has its limitations and drawbacks that are essential to understand for effective application.

Understanding the Regula Falsi Method

Before diving into its advantages and disadvantages, it's important to understand the basic concept of the regula falsi method.

Basic Concept

The regula falsi method is based on the idea of linear interpolation. Given a continuous function $f(x)$ and two points a and b such that $f(a)$ and $f(b)$ have opposite signs (indicating a root lies between them), the method approximates the root by drawing a straight line connecting the points $(a, f(a))$ and $(b, f(b))$. The intersection of this line with the x-axis provides a new approximation of the root, which then replaces either a or b based on the sign of the function at this intersection.

Step-by-Step Process

- Choose initial points a and b such that $f(a) \times f(b) < 0$
- Calculate the point c where the straight line connecting $(a, f(a))$ and $(b, f(b))$ intersects the x-axis:

[

$$c = b - \frac{f(b)(a - b)}{f(a) - f(b)}$$

]

- Evaluate $f(c)$. If $f(c)$ is sufficiently close to zero or within a desired tolerance, c is taken as the root.
- Otherwise, replace either a or b with c , depending on the sign of $f(c)$, and repeat the process.

Advantages of the Regula Falsi Method

Despite being a relatively simple numerical root-finding technique, the regula falsi method offers several notable advantages that make it appealing for various applications.

1. Simplicity and Ease of Implementation

- The regula falsi method relies on straightforward calculations involving linear interpolation, making it easy to implement even for beginners.
- No complex mathematical concepts or advanced programming skills are necessary, which allows for quick coding and testing.

2. Guaranteed Convergence under Certain Conditions

- When the initial interval $[a, b]$ contains a root and f is continuous, the method guarantees convergence to a root, provided the initial guesses are chosen appropriately.
- Unlike some methods, such as the secant method, the regula falsi method always converges if the initial bracketing is correct.

3. Faster than Bisection in Many Cases

- Since regula falsi uses linear interpolation, it often converges more rapidly than the bisection method, which simply bisects the interval regardless of the function's behavior.
- Especially when the function is well-behaved near the root, the method can achieve desired accuracy in fewer iterations.

4. No Need for Derivatives

- Unlike Newton-Raphson, the regula falsi method does not require the computation of derivatives, making it suitable for functions where derivatives are difficult or expensive to evaluate.

5. Suitable for Functions with Multiple Roots

- The method can be adapted to find multiple roots within a given interval by applying it iteratively over different subintervals.

Disadvantages of the Regula Falsi Method

While the regula falsi method has its merits, it also suffers from several significant drawbacks that can limit its effectiveness in certain scenarios.

1. Slow or Non-Uniform Convergence in Some Cases

- The method can experience "stalling" or very slow convergence when one endpoint remains fixed during iterations, especially if the function behaves poorly near the root.
- This occurs when the new approximation continually replaces only one endpoint, leading to a linear convergence rate similar to the bisection method rather than quadratic.

2. Dependence on Good Initial Brackets

- The success and efficiency of the method heavily depend on choosing initial points a and b such that $f(a)$ and $f(b)$ have opposite signs.
- Poor choices can lead to divergence, stagnation, or convergence to an incorrect root.

3. Potential for Stagnation

- In some cases, particularly with functions that are nearly flat or have multiple roots close to each other, the method may "stall," where the approximations do not improve significantly over iterations.
- This stagnation is problematic when quick convergence is desired.

4. Limited to Continuous Functions with Sign Changes

- The regula falsi method requires a continuous function with a known sign change over the interval. It is not suitable for functions that are discontinuous or do not satisfy this condition.
- Additional preliminary analysis is often necessary before applying the method.

5. Numerical Instability and Precision Issues

- When $f(a) \approx f(b)$, the denominator in the interpolation formula becomes very small, leading to potential numerical instability.
- This can cause inaccuracies or divergence in the root approximation, especially when working with floating-point arithmetic.

Features and Variants

To address some of the shortcomings of the basic regula falsi method, several variants have been developed:

- Illinois Method: Adjusts the weight of the fixed endpoint to improve convergence.
- Pegasus Method: Uses a modified interpolation formula for faster convergence.
- Modified Regula Falsi: Incorporates dynamic updates to endpoints to prevent stagnation.

Each of these variants aims to retain the simplicity of the original method while improving convergence speed and stability.

Practical Applications and Suitability

The regula falsi method is particularly useful in scenarios where:

- The function is continuous and the initial bracket is known.
- Derivative information is unavailable or expensive to compute.
- Quick implementation and results are required.

However, for functions with complex behavior, multiple roots, or where high precision is crucial, other methods like Newton-Raphson or secant might be more appropriate.

Conclusion

The regula falsi method remains a fundamental numerical technique for root-finding due to its simplicity and guaranteed convergence under the right conditions. Its strengths lie in its straightforward implementation, no requirement for derivatives, and often faster convergence than bisection, especially for well-behaved functions. Nevertheless, it faces notable challenges, such as potential slow convergence, stagnation issues, and sensitivity to the initial interval selection.

For practitioners, understanding both the advantages and limitations of the regula falsi method is vital for its effective application. When combined with strategic initial guesses and possible variants, it can serve as a powerful tool in the numerical analyst's toolkit. However, for more complex functions or demanding precision, alternative methods or hybrid approaches may offer better performance. Overall, the regula falsi method exemplifies the balance between simplicity and effectiveness in numerical root-finding techniques.

Question What are the main advantages of the regula falsi method? The regula falsi method is simple to implement, converges more reliably than some other methods for certain functions, and guarantees a root within the initial interval as long as the function is continuous and

the initial guesses bracket the root. What are the disadvantages of using the regula falsi method? One major disadvantage is that it can converge slowly, especially if the function is flat near the root, and it may get stuck with one endpoint not moving if the function's values at the interval ends do not change significantly. How does the regula falsi method compare to the bisection method in terms of efficiency? While the regula falsi method often converges faster than the bisection method due to its use of linear interpolation, it can sometimes suffer from slow convergence or stagnation, unlike the guaranteed steady convergence of bisection. Can the regula falsi method be used for all types of functions? The method works best for continuous functions where the initial interval brackets a root; however, for functions with multiple roots or discontinuities, its effectiveness may be limited or require modifications. What are some improvements or variants of the regula falsi method to overcome its disadvantages? Variants like the Illinois and Anderson methods introduce modifications to the regula falsi technique to accelerate convergence and prevent stagnation, making the root-finding process more efficient. Is the regula falsi method suitable for automated or iterative root-finding algorithms? Yes, it is suitable for automated algorithms due to its straightforward implementation, but care must be taken to monitor convergence speed and avoid stagnation, especially for challenging functions.

Related keywords: regula falsi method, false position method, numerical analysis, root finding, bracketing methods, convergence rate, advantages, disadvantages, iterative methods, computational efficiency

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